**Applecross Senior High School**

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**Western Australian Certificate of Education**

**Semester One Examination, 2018**

**Question/Answer Booklet**

**MATHEMATICS**

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97

**SPECIALIST**

**UNIT 1**

**Section Two:**

**Calculator- assumed Score for this booklet**

**Student’s Name**: **\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_**

**As shown on your exam timetable.**

**Student’s Teacher Mrs Waddell**

**Time allowed for this section**

Reading time before commencing work: ten minutes

Working time for this section: one hundred minutes

**Materials required/recommended for this section**

***To be provided by the supervisor***

This question /Answer Booklet

Formula Sheet (retained from Section One)

***To be provided by the candidate***

Standard Items: pens (blue/black preferred), pencils (including coloured), sharpener,

correction fluid/tape, eraser, ruler, highlighters.

Special items: drawing instruments, templates, notes on two unfolded sheets of A4 paper,

and up to three calculators approved for use in the WACE examinations.

**Important note to candidates**

No other items may be taken into the examination room. It is **your** responsibility to ensure

that you do not have any unauthorized notes or other items of a non-personal nature in the

examination room. If you have any unauthorized material with you, hand it to the supervisor

**before** reading any further.

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| --- | --- | --- | --- | --- | --- | --- |
| Section | Number of questions available | Number of questions to be answered | | Working time (minutes) | Marks available | Percentage of exam |
| Section One:  Calculator-free | 8 | 8 | | 50 | 53 | 35 |
| Section Two:  Calculator-assumed | 13 | 13 | | 100 | 97 | 65 |
|  | | | **Total** | | 150 | 100 |

## Instructions to candidates

1. The rules for the conduct of examinations are detailed in the *School Examination Rules* provided with your exam timetable.Sitting this examination implies that you agree to abide by these rules.
2. Write your answers in this Question/Answer Booklet.
3. You must be careful to confine your responses to the specific questions asked and to follow any instructions that are specific to a particular question.
4. Spare pages are included at the end of this booklet. They can be used for planning your responses and/or as additional space if required to continue an answer.

* Planning: If you use the spare pages for planning, indicate this clearly at the top of the page.
* Continuing an answer: If you need to use the space to continue an answer, indicate in the original answer space where the answer is continued, i.e. give the page number. Fill in the number of the question(s) that you are continuing to answer at the top of the page.

1. **Show all your working clearly**. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat an answer to any question, ensure that you cancel the answer you do not wish to have marked.
2. It is recommended that you **do not use pencil**, except in diagrams.
3. The formula sheet and your notes are **not to be handed** in with your Question/Answer Booklet.

Section Two: Calculator-assumed 65% (97 Marks)

This section has**thirteen (****13)** questions. Answer **all** questions. Write your answers in the spaces provided.

Working time: 100 minutes.

Question 9 (7 marks)

(a) A body travels with a velocity ms-1. Determine its speed and the bearing on which it is moving, assuming the positive -axis to be due north. (3 marks)

(b) Given that , determine the values of and .

(4 marks)

Question 10 (7 marks)

(a) Using the digits 0 to 9 inclusive, how many different five digit numbers can be made

if repetition of digits is allowed (1 mark)

(b) A number is divisible by four if the last two digits of the number is divisible by four. For example,

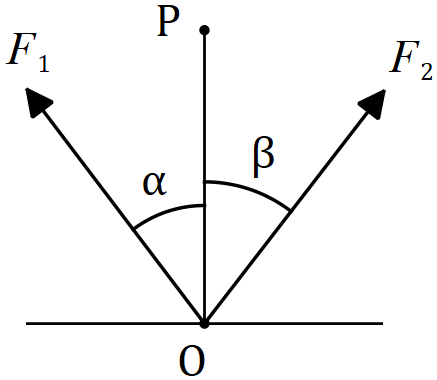
4564 is divisible by four because the last two digits “64” is divisible by four; but 4502 is not divisible by four because the last two digits “02” is not divisible by four. Again, using the digits 0 to 9 inclusive, find how many five digit numbers divisible by four can be formed

(i) if digits may be repeated (3 marks)

(ii) if no digit is to be repeated (3 marks)

Question 11 (8 marks)

Two forces, and , act on a body at , and make angles of and respectively with the vertical , as shown in the diagram below.



(a) Determine the magnitude of the resultant force and the angle it makes with the vertical.

(5 marks)

(b) The magnitude of is to be adjusted so that the direction of the resultant is vertical. Determine the required magnitude of . (3 marks)

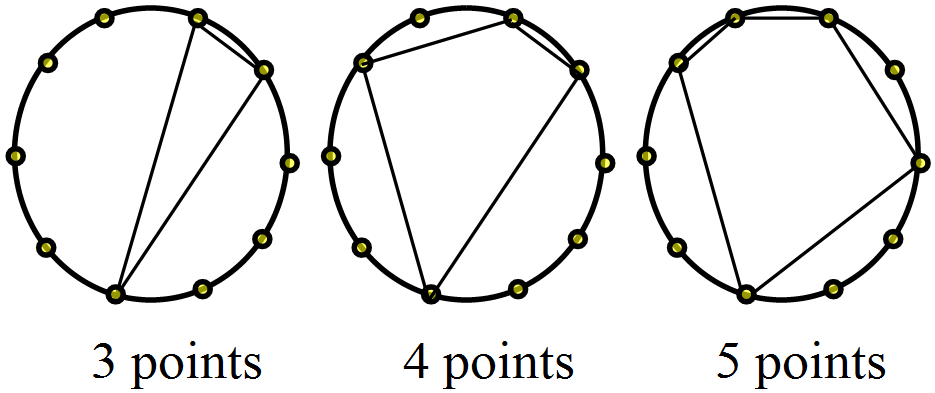
Question 12 (6 marks)

(a) Ten points are equally spaced around the circumference of a circle.

Determine the number of simple (non-self-intersecting) convex polygons that can be formed

by joining either three, four or five of these points with straight line segments

(as in the examples below). (2 marks)



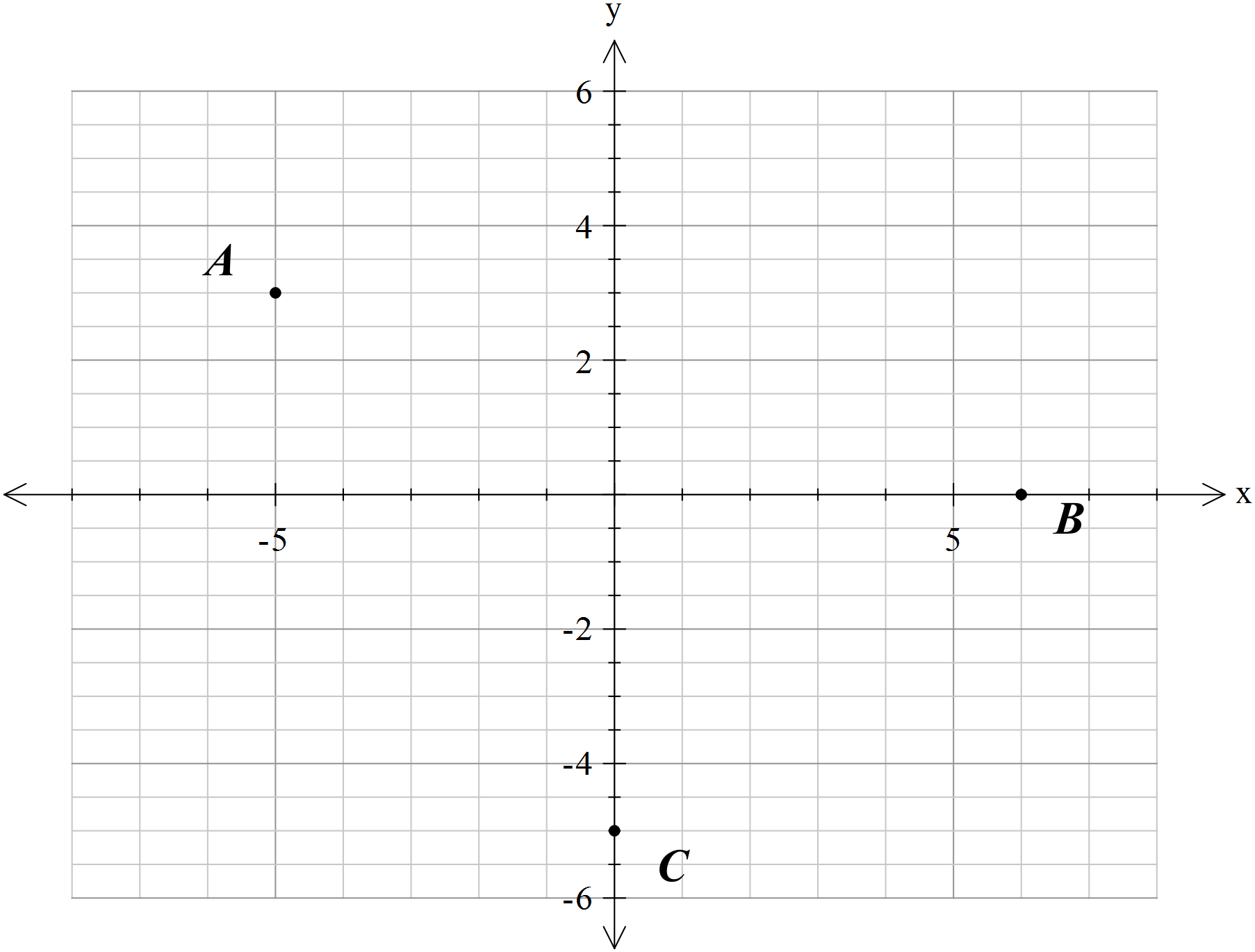
(b) A small coach has 24 seats, arranged in six rows of four seats each, with two seats in each row on either side of the central aisle. A group of passengers consisting of ten males and nine females board the bus.

(i) Determine how many combinations of empty seats are possible once everyone has sat down. (1 mark)

(ii) How many fewer combinations are there if the females all sit on one side of the aisle and the males all sit on the other side? (3 marks)

Question 13 (8 marks)

Consider the three points: A(-5,3), B(6,0) and C(0,-5).



1. Determine  in terms of  the horizontal and vertical unit vectors respectively. (1 mark)

Let K and L be the mid-points of AB and BC respectively.

(b) Without assuming any triangle properties, determine  in terms of . (3 marks)

The point B is now allowed to move freely along the axis, so has co-ordinates . Show that **p** and **q** are always parallel and that (4 marks)

Question 14 (8 marks)

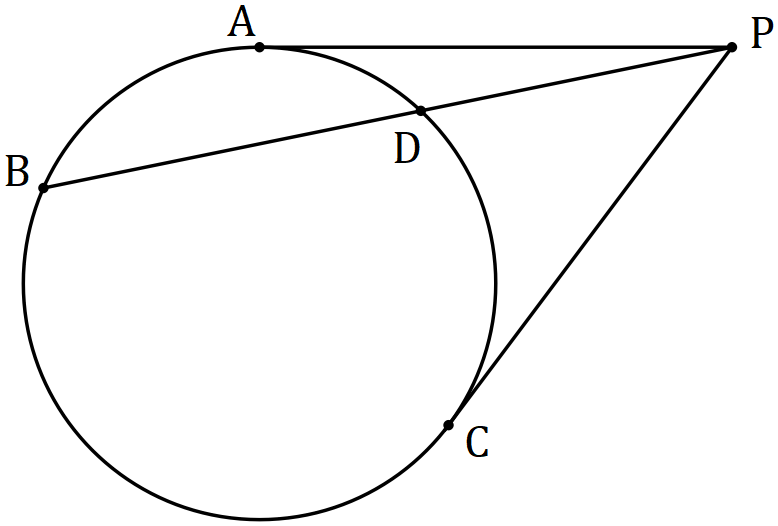
(a) Simplify given that and vector is parallel and in the opposite direction to vector . (4 marks)

(b) Using and , demonstrate a vector method to show that if the diagonals and of parallelogram are perpendicular, then the parallelogram is a rhombus.

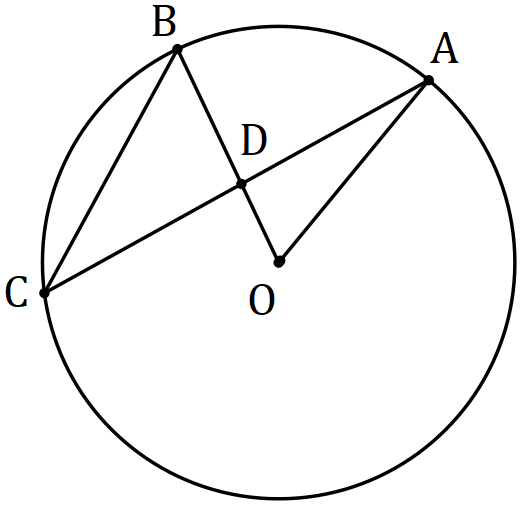
(4 marks)

Question 15 (9 marks)

(a) In the diagram below, and are tangents to the circle, with cm. Secant cuts the circle at , so that cm. Determine the lengths of and . (4 marks)



(b) In the diagram below, and lie on the circumference of the circle with centre , with intersecting at . Prove that . (5 marks)



Question 16 (9 marks)

(a) Determine the number of integers between and that are divisible by or .

(4 marks)

(b) A pigeon fancier has Florentine, King and Maltese pigeons and must choose three of them to enter in a local show. Determine the number of different ways the three pigeons can be chosen if

(i) there are no restrictions. (1 mark)

(ii) the fancier decides to take one of each breed. (2 marks)

(iii) the fancier decides to take at least two Maltese pigeons. (2 marks)

Question 17 (6 marks)

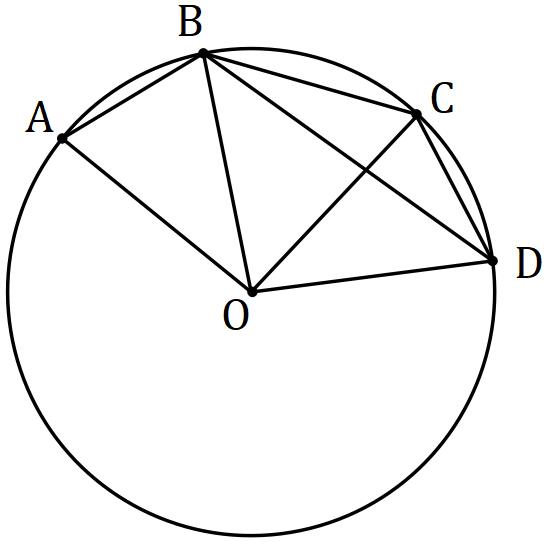
Three vectors are and .

(a) Determine the vector projection of on in exact form. (2 marks)

(b) If has the same magnitude as and is perpendicular to , determine the exact values of the coefficients and . (4 marks)

Question 18 (7 marks)

(a) In the diagram below, points and lie on the minor arc of the circle with centre . The lengths of chords and are congruent, and . Determine the size of . (3 marks)



(b) Line segment intersects line segment at . Given that and are non-parallel and the lengths and are 6, 41, 21 and 31 cm respectively, explain whether the points and are concyclic. (4 marks)

Question 19 (8 marks)

(a) Triangle has vertices with position vectors and . Point lies on side so that . Determine the vector . (4 marks)

(b) is a parallelogram. Point is the midpoint of side and point is on side so that . If and , determine in terms of and . (4 marks)

Question 20 (7 marks)

A small boat leaves jetty to travel to jetty , m away on a bearing of . A steady current of ms-1 runs in the river between the jetties on a bearing . If the small boat travels at a constant speed of ms-1, determine the bearing it should steer to reach jetty and how long the journey will take.

Question 21 (7 marks)

A child is playing with thirteen coloured cubes, all the same size. There are six pink cubes, three navy and one each of red, blue, orange and green.

(a) If the child stacks cubes one on top of another to make a column, determine the number of different coloured columns that can be made using

(i) all the red, blue and green cubes. (1 mark)

(ii) all the pink, red and orange cubes. (2 marks)

(iii) all the cubes. (2 marks)

(b) If all but one of the cubes are used to make a column, determine the number of different coloured columns that can now be made. Justify your answer. (2 marks)

**Additional working space.**

**Question Number: \_\_\_\_\_\_\_\_\_**